Math 123-01 Fall 2025 Dr. Lily Yen

## 

Name:
Number:
Signature:
Score: /30

**Problem 1**: Convert each of the following into Hindu-Arabic numeral base-10.

- a. 210123<sub>4</sub>
- b. T 4# 4#
- c. **> \$ \**
- a.  $2 \times 4^5 + 4^4 + 4^2 + 2 \times 4 + 3 = 2048 + 256 + 16 + 8 + 3 = 2331$ .
- b.  $2 \times 60^2 + 19 \times 60 + 16 = 8356$ .
- c.  $11 \times 20^2 + 17 \times 20 + 6 = 4746$ .

Score: /6

**Problem 2**: Convert 2574<sub>10</sub> to Mayan numerals.

$$2574 = 7 \times (18 \times 20) + 2 \times 20 + 14 =$$



Score: /2

**Problem 3**: We know that we have between 100 and 150 books in our STEM library. If we organize the books in groups of 9s, there are 2 left over; in groups of 7s, 4 books left over. How many books do we have?

Say you have a groups of 9 or b groups of 7. Then total number of books is 9a + 2 = 7b + 4. For example,  $9 \times 1 + 2 = 11 = 7 \times 1 + 4$ .

Since the lcm(9,7) = 63, there are 11 + 63 + 63 = 137 books in the STEM library.

Score: /2

**Problem 4**: On a Safari Hobby Farm, Farmer Jens has 5 ostriches, 2 zebras, and 3 gazelles. Suppose Farmer Jens needs to bring one of each kind of animals to an elementary school's fun fair, how many different groups of 3 (namely, an ostrich, a zebra, and a gazelle) are there?

 $5 \times 2 \times 3 = 30$  combinations of 3 different kinds of animals.

Score: /2

**Problem 5**: Sarbjit has 19 coins in her wallet which are either dimes (10-cent coins) or quarters (25-cent coins). She has a total of \$2.35 worth of coins in her wallet. How many dimes does Sarbjit have?

Say she has x dimes and 19-x quarters. Then the value in cents of her coins is

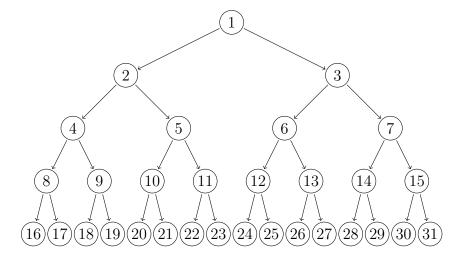
$$10x + 25(19 - x) = 235,$$

so 10x + 475 - 25x = 235, so -15x = 235 - 475 = -240, so x = 16.

Therefore Sarbjit has sixteen dimes and three quarters.

Score: /3

**Problem 6**: Shown is a binary tree organized in levels: Level 0 has 1 node; level 1 has 2 nodes (labelled 2 and 3); level 2 has 4 nodes (labelled 4, 5, 6, 7).



- a. How many nodes (circles) are in level 3?
- b. Which level of the tree contains the label 27?
- c. If you continue this pattern and draw the next level of the tree, what will the largest label be for the rightmost node?
- d. Which level of the tree contains the 4-digit label, 1234? Show your work.

Level 3 contains 8 nodes.

Level 4 contains the label 27.

The next level will be level 5 labelled from 32 to 63, so the rightmost node will be 63. Continuing with this pattern, we see that

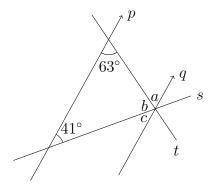
- level 6 has  $2^6 = 64$  nodes labelled 64 to 127;
- level 7 has  $2^7 = 128$  nodes (128 to 255),
- level 8 has  $2^8 = 256$  nodes (256 to 511),
- level 9 has  $2^9 = 512$  nodes (512 to 1023),
- level 10 has  $2^{10} = 1024$  nodes (1024 to 2047).

Therefore, the label, 1234 is found on Level 10.

Score: /5

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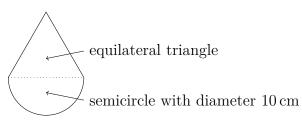
**Problem 7**: Lines p and q are parallel. Lines s and t are transversals. Find the measures of angles a, b, and c.



$$c = 41^{\circ}$$
,  $a = 63^{\circ}$ , and  $b = 180^{\circ} - 41^{\circ} - 63^{\circ} = 76^{\circ}$ .

Score: /3

**Problem 8**: Shown is an equilateral triangle with its base equal to the diameter of a semicircle. If the diameter is 10 cm, find both the perimeter and the area of the figure.



Perimeter is  $10 + 10 + 2\pi \times 5/2 = 20 + 5\pi$  centimetres.

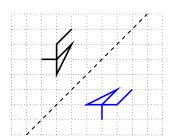
The area of the semicircle is  $\pi 5^2/2 = \frac{25\pi}{2}$  while the triangle area is  $\frac{1}{2} \times 10 \times 5\sqrt{3} = 25\sqrt{3}$ ; so the combined area is  $\frac{25\pi}{2} + 25\sqrt{3}$  square cm.

Score: /5

**Problem 9**: Find the measure of one interior angle of a regular dodecagon (12-sided).  $(12-2) \times 180^{\circ}/12 = 150^{\circ}$ .

Score: /1

**Problem 10**: Reflect the given figure along the dashed line.



Score: /1

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