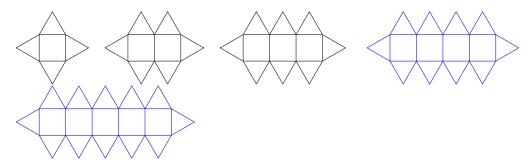
Math 123-01 Summer 2025 Dr. Lily Yen

Midterm I Show all your work

Name:		
Number:		
Signature:		
Score:	/30	

Problem 1: Using matchsticks, we create shapes in the following pattern. From the left, we see the first, the second, and the third.



- a. Draw the 4th and the 5th shapes.
- b. Draw a table of values showing a pattern for the number of matchsticks used in the first four shapes?

Shape #	1	2	3	4	5	 \overline{n}
Matchsticks	12	19	26	33	40	 7n + 5

c. How many match sticks are in the nth shape? Express your formula in terms of n.

The *n*th shape has 2 + 2n triangles that contribute 3(2 + 2n) matchsticks. In addition, we find n - 1 vertical sticks. The total is therefore

$$3(2+2n) + n - 1 = 7n + 5.$$

Score: /5

Problem 2: Anjali goes on a trip and packs 3 different tops, 4 different skirts, and 5 different pairs of shoes. How many different outfits can Anjali wear on this trip by choosing one top,

one skirt, and one pair of shoes?

60

 $3 \times 4 \times 5 = 60$ outfits.

Score:

/2

Problem 3: Yuja has 19 coins in her wallet which are either nickels (5-cent coins) or quarters (25-cent coins). She has a total of \$3.35 worth of coins in her wallet. How many nickels does Yuja have?

Say she has x nickels and 19-x quarters. Then the value in cents of her coins is

$$5x + 25(19 - x) = 335,$$

so 5x + 475 - 25x = 335, so -20x = 335 - 475 = -140, so x = 7. Therefore Yuja has **seven nickels** and twelve quarters.

Score: /3

Problem 4: Convert each of the following into Hindu-Arabic numeral base-10.

a. 11101001₂

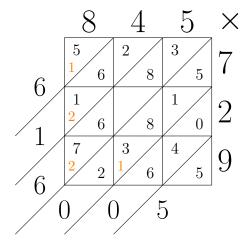
a.
$$2^7 + 2^6 + 2^5 + 2^3 + 2^0 = 128 + 64 + 32 + 8 + 1 = 233$$
.

b.
$$2 \times 60^2 + 34 \times 6 + 11 = 9251$$
.

c.
$$8 \times 20^2 + 5 \times 20 + 6 = 3306$$
.

Score: /5

Problem 5: Multiply 845×729 using the galley method.



Score: /2

Problem 6: We know that we have between 150 and 200 books in our STEM library. If we organize the books in groups of 7s, there are 2 left over; in groups of 6s, 4 books left over. How many books do we have?

Say you have a groups of 7 or b groups of 6. Then total number of books is 7a + 2 = 6b + 4. For example, $7 \times 2 + 2 = 16 = 6 \times 2 + 4$.

a =	2	8	14	20	26	32
b =	2	9	16	23	30	37
Total $7a + 2 = 6b + 4 =$	16	58	100	142	184	226

So the STEM library has 184 books.

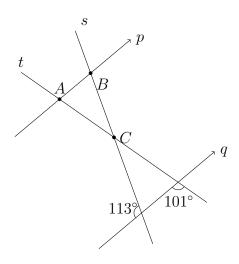
Score: /3

/10

Problem 7: Lines p and q are parallel. Lines s and t are transversals. Find the measures

of interior angles in $\triangle ABC$: $\angle BAC = \begin{bmatrix} 79^{\circ} \\ \end{bmatrix}$, $\angle ABC = \begin{bmatrix} 67^{\circ} \\ \end{bmatrix}$, and

$$\angle \mathit{ACB} = \boxed{34^\circ}$$



Score: /3

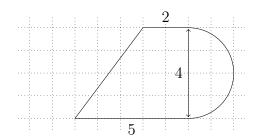
Problem 8: We have a slice of a circular pie with a diameter of 10 cm. The area of this slice is 30 cm^2 . What is the perimeter of this slice?



Since the diameter is 10 cm, the radius is r=5 cm. The area of the whole circle is $\pi r^2=25\pi\,\mathrm{cm}^2$, so the sector is $\frac{30}{25\pi}=\frac{6}{5\pi}$ of the circle. The circumference of the whole circle is $2\pi r=10\pi\,\mathrm{cm}$, so the length of the sector arc is $\frac{6}{5\pi}\times10\pi\,\mathrm{cm}=12\,\mathrm{cm}$. Therefore the perimeter of the sector is $2r+12\,\mathrm{cm}=22\,\mathrm{cm}$.

Score: /3

Problem 9: We have a lot in the following shape consisting of a trapezoid with bases of lengths 2 and 5 that has a semicircle of diameter 4 attached to its side. Find its area and perimeter.



a. For area:

The radius of the semicircle is 2, so the total area is

$$\frac{2+5}{2} \times 4 + \frac{1}{2} \times \pi 2^2 = 14 + 2\pi \approx 20.28$$

b. For perimeter:

The slanted line has length $\sqrt{3^2 + 4^2} = \sqrt{25} = 5$, so the perimeter is

$$5 + 5 + 2 + \frac{1}{2} \times 2\pi^2 = 12 + 2\pi \approx 18.28$$

Score: /4

/10

Page 3 Math 123-01