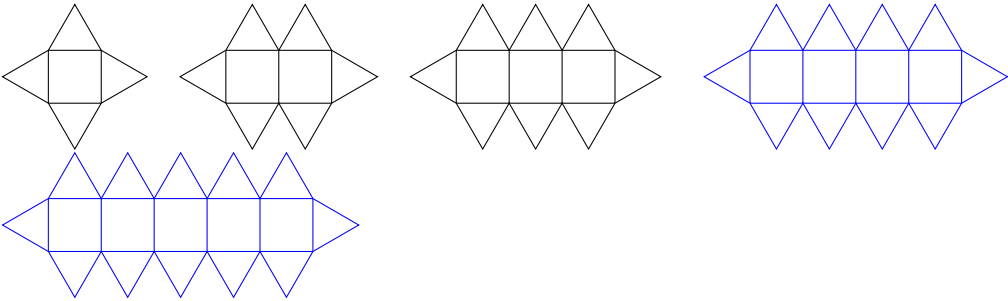


Problem 1: Using matchsticks, we create shapes in the following pattern. From the left, we see the first, the second, and the third.



- a. Draw the 4th and the 5th shapes.
- b. Draw a table of values showing a pattern for the number of matchsticks used in the first four shapes?

Shape #	1	2	3	4	5	...	n
Matchsticks	12	19	26	33	40	...	$7n + 5$

- c. How many matchsticks are in the n th shape? Express your formula in terms of n .

The n th shape has $2 + 2n$ triangles that contribute $3(2 + 2n)$ matchsticks. In addition, we find $n - 1$ vertical sticks. The total is therefore

$$3(2 + 2n) + n - 1 = 7n + 5.$$

Problem 2: Anjali goes on a trip and packs 3 different tops, 4 different skirts, and 5 different pairs of shoes. How many different outfits can Anjali wear on this trip by choosing one top, one skirt, and one pair of shoes?

$3 \times 4 \times 5 = 60$ outfits.

Score: ____/5

60

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Problem 3: Yuja has 19 coins in her wallet which are either nickels (5-cent coins) or quarters (25-cent coins). She has a total of \$3.35 worth of coins in her wallet. How many nickels does Yuja have?

Say she has x nickels and $19 - x$ quarters. Then the value in cents of her coins is

$$5x + 25(19 - x) = 335,$$

so $5x + 475 - 25x = 335$, so $-20x = 335 - 475 = -140$, so $x = 7$.
Therefore Yuja has **seven nickels** and twelve quarters.

Score: ____/2

Score: ____/3

Problem 7: Lines p and q are parallel. Lines s and t are transversals. Find the measures of INTERIOR ANGLES in $\triangle ABC$: $\angle BAC =$

79°

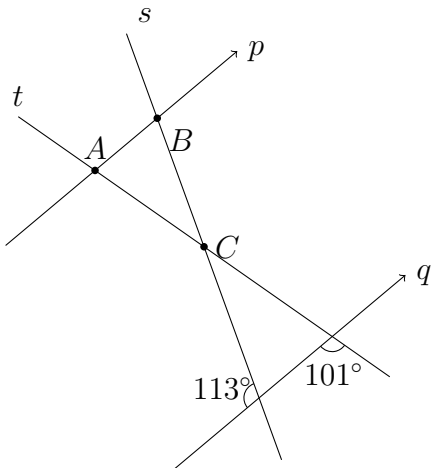
 $,$ $\angle ABC =$

67°

 $,$ and $\angle ACB =$

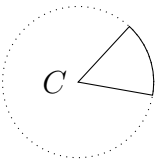
34°

 $.$



Score: /3

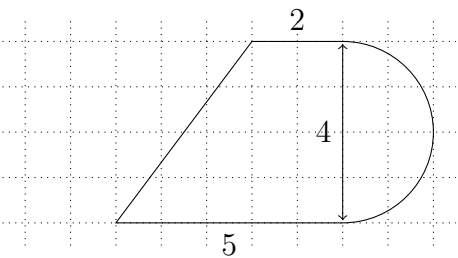
Problem 8: We have a slice of a circular pie with a diameter of 10 cm. The area of this slice is 30 cm^2 . What is the perimeter of this slice?



Since the diameter is 10 cm, the radius is $r = 5\text{ cm}$. The area of the whole circle is $\pi r^2 = 25\pi\text{ cm}^2$, so the sector is $\frac{30}{25\pi} = \frac{6}{5\pi}$ of the circle. The circumference of the whole circle is $2\pi r = 10\pi\text{ cm}$, so the length of the sector arc is $\frac{6}{5\pi} \times 10\pi\text{ cm} = 12\text{ cm}$. Therefore the perimeter of the sector is $2r + 12\text{ cm} = 22\text{ cm}$.

Score: /3

Problem 9: We have a lot in the following shape consisting of a trapezoid with bases of lengths 2 and 5 that has a semicircle of diameter 4 attached to its side. Find its area and perimeter.



a. For area:

The radius of the semicircle is 2, so the total area is

$$\frac{2+5}{2} \times 4 + \frac{1}{2} \times \pi 2^2 = 14 + 2\pi \approx 20.28$$

b. For perimeter:

The slanted line has length $\sqrt{3^2 + 4^2} = \sqrt{25} = 5$, so the perimeter is

$$5 + 5 + 2 + \frac{1}{2} \times 2\pi 2 = 12 + 2\pi \approx 18.28$$

Score: /4