Math 123 Spring 2023 Dr. Lily Yen

## Assignment 4

Show all your work

Name: Number: Signature: Score: /21

**Problem 1**: Answer the questions. Write out steps for each. One mark per part except two marks for the last part.

a. Convert the fraction three and nine tenths into a percent.

 $3\frac{9}{10} = 3.9 = 390\%$ 

b. Find 0.8% of 278.

 $0.008 \times 278 = 2.224$ 

c. Brian wants to share 6 mini-snack bars out of a box of 120 with his brothers. What 5%percentage of his box of mini-snack bars does he want to share?

 $\frac{6}{120} = 0.05 = 5\%$ 

d. If Janette finds in her drawer 34 % of her pens are Muji pens, and she counts 17 Muji

pens in total, how many pens does she have in her drawer?

bU pens

If 0.34x = 17, then  $x = \frac{17}{0.34} = 50$ 

e. David's family attended Love and Fate, a concert by the Vancouver Brass Orchestra last fall. For the family dinner before the concert, David's grandmother paid \$279 including taxes and an 18 % tip. What was bill before taxes and tip? Assume a 12 %

service tax.

If the bill was x, then the tax was 0.12x and the tip was 0.18x, so he paid x + 0.12x + 0.18x = 1.30x = 279, so  $x = \frac{$279}{1.30} = $214.615$ . Therefore the bill before taxes and tip was \$214.62.

> Score: /6

**Problem 2**: Solve for the indicated variable in each of the following.

a. Solve for I in  $m = \frac{P+I}{n}$ 

If  $m = \frac{P+I}{n}$ , then mn = P+I, so I = mn-P.

b. Solve for x in  $(1.24)^x = 10$ . Provide accuracy to two decimal places.

If  $(1.24)^x = 10$ , then  $\log((1.24)^x) = \log(10)$ , so  $x \log(1.24) = \log(10)$ , so  $x = \frac{\log(10)}{\log(1.24)} \approx 10.70.$ 

c. Solve for r in  $A = P(1+r)^7$ 

If  $A = P(1+r)^7$ , then  $A/P = (1+r)^7$ , so  $(A/P)^{1/7} = 1+r$ , so  $r = (A/P)^{1/7} - 1$ 

**Problem 3**: Janette's grandmother is offered by her bank three options for a \$6000 guaranteed investment certificate (GIC):

- a. 4.5% compounded monthly;
- b. 4.55% compounded annually; or
- c.  $4.33\,\%$  compounded weekly. (Use 52 weeks per year.)

Compute the interest after one year in each case and decide which option earns Janette's grandmother the most.

- a.  $\$6000(1 + \frac{0.045}{12})^{12} = \$6275.64$ , so the interest is \$275.64.
- b.  $\$6000 \times 0.0455 = \$273.00$
- c.  $\$6000(1 + \frac{0.0433}{52})^{52} = \$6265.39$ , so the interest is \$265.39.

Hence the 4.5% compounded monthly (option a) is best.

Score: /5

**Problem 4**: Brian's cousin purchased a sailboat and financed \$8500 at \$650 per month for 18 months. Assuming the add-on interest method, what was the amount of interest paid over 18 months? Find the annual interest rate charged on the loan.

Brian's cousin paid a total of  $18 \times \$650 = \$11700$ . Since they borrowed \$8500, the total interest paid was \$3200.

To find the annual interest rate,  $3200 \div 8500 \div 1.5 \approx 0.25098$ , so around 25 %.

core: /3

**Problem 5**: If *Chancellor's Choice Financial* master card charges 22 % on unpaid balance, how much would it cost in finance charge to leave \$757 unpaid past the due date for 30 days? Hint: Credit card companies use 365 days a year. For the sake of simplicity, use simple interest.

$$\$757 \times \frac{0.22}{365} \times 30 \approx \$13.69$$

Score: /2