Name:

Math 123
Spring 2023
Dr. Lily Yen
$\underset{\substack{\text { Show all your work }}}{\substack{\text { Sisignent }}}$

Number:
Signature:
Score: $\qquad$

Problem 1: Answer the questions. Write out steps for each. One mark per part except two marks for the last part.
a. Convert the fraction three and nine tenths into a percent.
$3 \frac{9}{10}=3.9=390 \%$
b. Find $0.8 \%$ of 278 .
$0.008 \times 278=2.224$
c. Brian wants to share 6 mini-snack bars out of a box of 120 with his brothers. What percentage of his box of mini-snack bars does he want to share?
$\frac{6}{120}=0.05=5 \%$
d. If Janette finds in her drawer $34 \%$ of her pens are Muji pens, and she counts 17 Muji pens in total, how many pens does she have in her drawer?

If $0.34 x=17$, then $x=\frac{17}{0.34}=50$
e. David's family attended Love and Fate, a concert by the Vancouver Brass Orchestra last fall. For the family dinner before the concert, David's grandmother paid $\$ 279$ including taxes and an $18 \%$ tip. What was bill before taxes and tip? Assume a $12 \%$ service tax.

If the bill was $\$ x$, then the tax was $0.12 x$ and the tip was $0.18 x$, so he paid $x+0.12 x+0.18 x=1.30 x=279$, so $x=\frac{\$ 279}{1.30}=\$ 214.615$. Therefore the bill before taxes and tip was $\$ 214.62$.

Problem 2: Solve for the indicated variable in each of the following.
a. Solve for $I$ in $m=\frac{P+I}{n}$ If $m=\frac{P+I}{n}$, then $m n=P+I$, so $I=m n-P$.
b. Solve for $x$ in $(1.24)^{x}=10$. Provide accuracy to two decimal places.

If $(1.24)^{x}=10$, then $\log \left((1.24)^{x}\right)=\log (10)$, so $x \log (1.24)=\log (10)$, so $x=\frac{\log (10)}{\log (1.24)} \approx 10.70$.
c. Solve for $r$ in $A=P(1+r)^{7}$

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\begin{aligned}
& \text { If } A=P(1+r)^{7} \text {, then } A / P=(1+r)^{7} \text {, so }(A / P)^{1 / 7}=1+r \text {, so } \\
& r=(A / P)^{1 / 7}-1
\end{aligned}
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Problem 3: Janette's grandmother is offered by her bank three options for a $\$ 6000$ guaranteed investment certificate (GIC):
a. $4.5 \%$ compounded monthly;
b. $4.55 \%$ compounded annually; or
c. $4.33 \%$ compounded weekly. (Use 52 weeks per year.)

Compute the interest after one year in each case and decide which option earns Janette's grandmother the most.
a. $\$ 6000\left(1+\frac{0.045}{12}\right)^{12}=\$ 6275.64$, so the interest is $\$ 275.64$.
b. $\$ 6000 \times 0.0455=\$ 273.00$
c. $\$ 6000\left(1+\frac{0.0433}{52}\right)^{52}=\$ 6265.39$, so the interest is $\$ 265.39$.

Hence the $4.5 \%$ compounded monthly (option a) is best.

Score: /5
Problem 4: Brian's cousin purchased a sailboat and financed $\$ 8500$ at $\$ 650$ per month for 18 months. Assuming the add-on interest method, what was the amount of interest paid over 18 months? Find the annual interest rate charged on the loan.

Brian's cousin paid a total of $18 \times \$ 650=\$ 11700$. Since they borrowed $\$ 8500$, the total interest paid was $\$ 3200$.
To find the annual interest rate, $3200 \div 8500 \div 1.5 \approx 0.25098$, so around $25 \%$.

Problem 5: If Chancellor's Choice Financial master card charges $22 \%$ on unpaid balance, how much would it cost in finance charge to leave $\$ 757$ unpaid past the due date for 30 days? Hint: Credit card companies use 365 days a year. For the sake of simplicity, use simple interest.

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\$ 757 \times \frac{0.22}{365} \times 30 \approx \$ 13.69
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