

Problem 1: Answer each question to two decimal places when appropriate. Steps may help with part marks.

- a. Find 61.3 % of 720.

441.36

$0.613 \times 720 = 441.36$

- b. Convert the fraction $4\frac{2}{9}$ into a percent.

422.2 %

$4\frac{2}{9} = 4 + \frac{2}{9} = \frac{38}{9} \approx 4.222 = 422.2 \%$

- c. When David buys a 400-dollar (ticket price) snowboard, how much does the store charge David in taxes? Hint: Stores need to charge a 5 % GST and a 7 % PST.

\$48

12% of \$400 is $0.12 \times 400 = 48$.

- d. Janette treated her mother to a Mother’s Day Brunch at Queen Elizabeth’s Theatre’s Browns Social House. She saved \$90 for this occasion to cover a 15 % tip and a 12 % service tax. What was the maximum they could order to stay within her budget of \$90?

\$70.86

Say the cost before tip and taxes is $\$x$. Then the tip is $0.15x$, and the tax is $0.12x$, so he has to pay $x + 0.15x + 0.12x = 1.27x$. If $1.27x = \$90$, then $x = \frac{90}{1.27} = \$70.86$.

- e. The residents of a small town and the surrounding areas are divided over the proposed construction of a new waste management station in town, as shown in the table. A reporter randomly selects a person to interview from a group of residents. If the person selected lives in town, what is the probability that the person opposes the new waste management station?

	Support new station	Oppose new station
Live in town	252	6369
Live in surrounding areas	7518	416

96.2 %

$\frac{6369}{252+6369} = \frac{6369}{6621} \approx 0.962 = 96.2 \%$

Score: /5

Problem 2: Solve for the indicated variable.

- a. Solve for t in $A = P(1 + rt)$

If $A = P(1 + rt)$, then $\frac{A}{P} = 1 + rt$, so $rt = \frac{A}{P} - 1$, so

- b. Solve for x in $(2.8)^x = 32$ $t = \frac{\frac{A}{P} - 1}{r} = \frac{\frac{A-P}{P}}{r} = \frac{A - P}{Pr}$

If $(2.8)^x = 32$, then $\log((2.8)^x) = \log(32)$, so $x \log(2.8) = \log(32)$, so $x = \frac{\log(32)}{\log(2.8)} \approx 3.366$

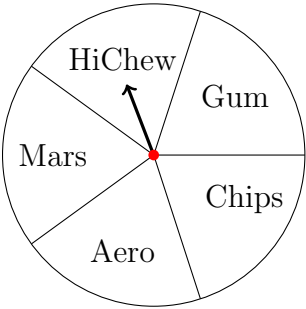
- c. Solve for r in $A = P(1 + r/m)^n$

If $A = P(1 + r/m)^n$, then $\frac{A}{P} = (1 + r/m)^n$, so $(A/P)^{1/n} = 1 + r/m$, so $(A/P)^{1/n} - 1 = r/m$, so

$r = m \left(\left(\frac{A}{P} \right)^{1/n} - 1 \right) = m \sqrt[n]{A/P} - m$

Score: /5

Problem 3: Dad constructed a spinner with five equal sectors the morning after Halloween for Hamlet and Samlet. Assume that the pointer never lies on a border line, answer the following questions.



- a. State the sample space for spinning the spinner once.
- $S = \{\text{Gum, Chips, Aero, Mars, HiChew}\}$
- b. Find the probability for the event of getting at least one Mars after two spins.

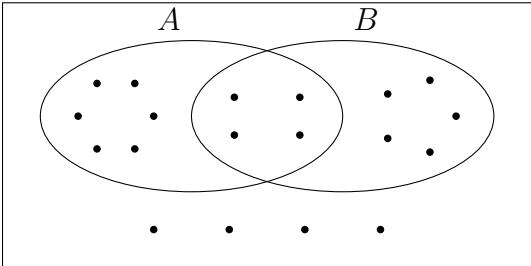
The chance of not getting any Mars's in two spins is $(\frac{4}{5})^2 = \frac{16}{25}$, so the chance of at least one is $1 - \frac{16}{25} = \frac{9}{25} = 0.36 = 36\%$.

- c. Find the probability for the event of getting no Chips after three spins.

The chance of zero Chips is $(\frac{4}{5})^3 = \frac{64}{125} = 0.512 = 51.2\%$.

Score: /5

Problem 4: Dad drew a big rectangle representing a sample space containing two events, A and B . Assume that the outcomes (as dots) were all equally likely, answer the following questions.



- a. $P(A \cap B)$
- b. $P(\bar{A})$
- c. $P(B \cup \bar{A})$
- d. $P(B \mid A)$
- e. Are A and B mutually exclusive?

$\frac{4}{19} \approx 21.1\%$

$\frac{9}{19} \approx 47.4\%$

$\frac{13}{19} \approx 68.4\%$

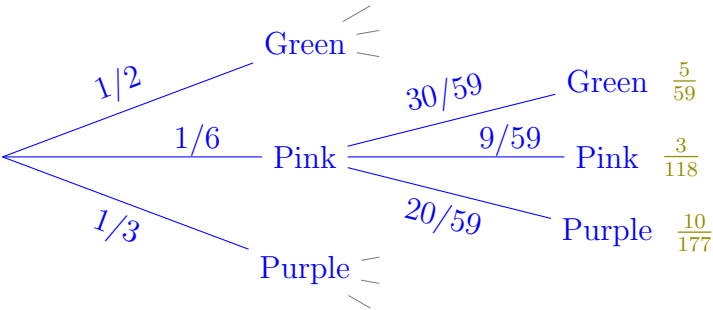
$\frac{4}{10} = 40.0\%$

$A \cap B \neq \emptyset$, so A and B are *not* mutually exclusive.

Score: /5

Problem 5: A candy jar contains 30 green jelly beans, 10 pink jelly beans, and 20 purple jelly beans. Two jelly beans are randomly selected without replacement. Let P be the event *you select a pink jelly bean first*, and let N be the event *the second jelly bean is not purple*.

- Find the probability that the first jelly bean is NOT purple. $\frac{1}{2} + \frac{1}{6} = \frac{2}{3}$
- Find $P(N \mid P)$ with a probability tree.



Therefore,

$$P(N \mid P) = \frac{P(N \text{ and } P)}{P(P)} = \frac{\frac{5}{59} + \frac{3}{118}}{\frac{1}{6}} = \frac{\frac{13}{118}}{\frac{1}{6}} = \frac{39}{59} \approx 0.661 = 66.1 \%$$

Score: /4

Problem 6: Suppose Brian’s brother purchased a used sail boat for \$4000 and agreed to pay off the boat in 18 monthly payments of \$350 each.

- Find the total amount of interest charged in this boat loan.

He paid a total of $18 \times \$350 = \6300 , so the interest was $\$6300 - \$4000 = \$2300$.

- Assume the payments were computed using the add-on interest method; find the annual interest rate applied.

With the add-on method, $I = Prt$, so $r = \frac{I}{Pt} = \frac{\$2300}{\$4000 \times 1.5} \approx 0.3833 = 38.33 \%$

Score: /3

Problem 7: David’s grandparents want to establish a fund for their grandchildren’s uni-versity education. What lump sum must they deposit at a 2.5 % annual interest rate, com-pounded monthly, in order to have \$20 000 in the fund at the end of 18 years?

If

$$\$20\,000 = P \left(1 + \frac{2.5 \, \%}{12} \right)^{18 \times 12} = P(1.002\,083)^{216},$$

then $P = \frac{\$20\,000}{(1.002\,083)^{216}} \approx \$12\,758.53$.

Score: /3